

Problem 14

Solve for x :

$$\sqrt{x\sqrt{x}} - 2\sqrt[3]{x\sqrt{x}} = 0, \quad x \neq 0$$

Answer

64

Explanation

$$\sqrt{x^{4/3}} - 2\sqrt[3]{x^{3/2}} = 0$$

$$x^{2/3} - 2x^{1/2} = 0$$

$$x^{1/2} (x^{1/6} - 2) = 0$$

$$\begin{array}{l|l} x^{1/2} = 0 & x^{1/6} - 2 = 0 \\ & x^{1/6} = 2 \\ & x = 2^6 \\ x = 0 & x = 64 \end{array}$$

$$\Rightarrow x = 64$$